

# Structural Damage Detection in Plates Using Wavelet Theories

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## Abstract

The study of structural damage detection in thin plates using wavelet theories and transforms is motivated by the critical need for robust methodologies to ensure the safety and reliability of civil and mechanical infrastructure. Traditional methods of damage detection, reliant on visual inspections or conventional sensors, often fall short in capturing subtle or localized damage, thereby necessitating more advanced techniques. In recent years, wavelet analysis has emerged as a promising tool due to its ability to provide multi-resolution analysis, capturing both global and localized damage, as well as its capability to accurately capture transient dynamic responses.

The primary objective of this thesis is to develop a comprehensive methodology for structural damage detection in plates using wavelet theories and transforms. This involves investigating the theoretical foundations of wavelet analysis, developing algorithms and computational tools for wavelet-based damage detection, conducting experimental studies to validate the methodology, and comparing its effectiveness with conventional methods. The scope of the research encompasses various types of damage, including cracks, delamination, and degradation, in thin plates, with consideration given to different plate geometries and boundary conditions.

Structural Health Monitoring (SHM) plays a crucial role in ensuring the safety, reliability, and longevity of engineering structures. By continuously monitoring the condition of structures, SHM systems can detect damage early, allowing for timely intervention to prevent catastrophic failures. Moreover, SHM facilitates cost savings, extends the service life of structures, reduces environmental impact, and enables informed decision-making regarding maintenance and resource allocation.

State-of-the-art SHM techniques include sensor networks, non-destructive testing, machine learning, wireless monitoring, acoustic emission testing, fiber-optic sensing, and digital twins. These techniques have revolutionized the field, enabling more effective monitoring and maintenance of structures, thereby enhancing safety and sustainability in the built environment.

Date of Submission: 27-06-2024

Date of acceptance: 06-07-2024

## I. INTRODUCTION

Generally, underlying harm identification has been a difficult undertaking, frequently depending on visual reviews or regular strategies like strain measures and accelerometers. While these strategies have their benefits, they may not be reasonable for consistent, ongoing checking, and they may not successfully catch unobtrusive, limited harm. This limit has driven analysts to investigate inventive and high level strategies for more precise, dependable, and productive harm location techniques.

Lately, wavelet speculations and changes have arisen as promising devices for underlying harm location. Wavelet investigation offers interesting benefits, for example, multi-goal examination, which empowers the discovery of both worldwide and confined harm, and the capacity to catch transient powerful reactions with high

accuracy. These capacities make wavelet-based methods profoundly significant for evaluating the primary soundness of different parts, especially slight plates, which are vital pieces of many designing frameworks, including extensions, airplane, and structures.

The inspiration driving this exploration comes from the developing requirement for strong, productive, and exact harm location philosophies, particularly for slim plates. This study expects to use wavelet speculations and changes to propel the field of underlying harm discovery by creating pragmatic and viable devices for distinguishing harm in plate-like designs. Thusly, we add to the continuous endeavors to improve the security and unwavering quality of basic foundation frameworks.

The primary objective of this thesis is to develop a comprehensive methodology for structural damage

detection in plates using wavelet theories and transforms. This research seeks to:

1. Investigate the theoretical foundations of wavelet theories and transforms in the context of structural health monitoring.
2. Develop algorithms and computational tools for wavelet-based damage detection in plate-like structures.
3. Perform experimental studies to validate the proposed methodology and assess its performance under various conditions.
4. Compare the effectiveness of wavelet-based approaches with conventional methods for damage detection in thin plates.
5. Provide recommendations for the practical application of wavelet theories in real-world structural health monitoring systems.

The extent of this proposition envelops a careful investigation of wavelet hypotheses and changes as they connect with the recognition of underlying harm in flimsy plates. This exploration will research the pertinence of wavelet-based techniques to various kinds of harm, including breaks, delamination, and different types of weakening. The review will likewise consider different plate calculations and limit conditions to evaluate the flexibility and versatility of the proposed procedure.

While this examination essentially centers around slim plates, the ideas and discoveries might have more extensive ramifications for underlying wellbeing checking in an assortment of designing frameworks. The result of this study will add to the continuous advancement of primary harm location strategies and may make ready for additional dependable and productive techniques in the field of common and mechanical designing.

## II. LITERATURE REVIEW

The integration of wavelet transform in Structural Health Monitoring (SHM) for plate structures represents a significant advancement in ensuring the safety and longevity of critical infrastructure. This literature review synthesizes existing research on wavelet transform, SHM, and plate structures, highlighting gaps in the literature and providing a rationale for the current study's focus.

Wavelet transform has emerged as a powerful mathematical tool with applications across various fields, including signal analysis, image processing, and structural health monitoring. Unlike traditional Fourier transform, which provides frequency domain information, wavelet transform operates in both time and frequency domains,

offering a unique perspective on data analysis. Its ability to capture localized features and time-varying behavior makes it particularly suitable for analyzing structural responses and detecting damage in plate structures.

Structural Health Monitoring (SHM) is a critical discipline in engineering aimed at continuously monitoring the condition of structures to ensure their safety and reliability. SHM techniques involve the use of sensors, data analysis algorithms, and assessment methods to detect, assess, and mitigate structural damage or deterioration. The importance of SHM lies in its ability to enable proactive maintenance and prevent catastrophic failures, thereby enhancing safety and reducing maintenance costs.

Plate structures are integral components in various engineering applications, including bridges, aircraft, buildings, pressure vessels, and marine vessels. These structures are susceptible to various forms of damage, such as fatigue cracking, corrosion, delamination, and material degradation, which can compromise their integrity and performance over time. Monitoring the health of plate structures is essential for identifying damage early, assessing its severity, and implementing timely repairs or maintenance measures.

Despite the advancements in SHM techniques, there are several gaps in the existing literature regarding the application of wavelet transform in SHM for plate structures:

1. **Limited Application in Plate Structures:** While wavelet transform has been widely used in SHM for different structural types, its specific application to plate structures is relatively limited. Existing research primarily focuses on other structural forms, such as beams, frames, and trusses, leaving a gap in understanding the full potential of wavelet transform for plate structure health monitoring.
2. **Insufficient Multiresolution Analysis:** Multiresolution analysis is a fundamental concept in wavelet transform, allowing for the identification of structural behaviors at different scales. However, there is a lack of comprehensive studies leveraging wavelet transform's multiresolution analysis capabilities to capture the diverse behaviors exhibited by plate structures under varying loading conditions.
3. **Challenges in Implementation:** Practical challenges related to implementing wavelet transform in SHM for plate structures are not well-documented in the literature. These challenges may include sensor placement, data quality assurance, computational demands, interpretation of results, and integration with existing monitoring systems.

4. **Lack of Comprehensive Case Studies:** While there are examples of wavelet transform applications in SHM, there is a scarcity of comprehensive case studies demonstrating its effectiveness in addressing practical issues specific to plate structures. Comprehensive case studies are essential for validating the reliability and applicability of wavelet transform-based SHM approaches in real-world scenarios.

5. **Integration of Recent Developments:** Recent advancements in wavelet transform, such as data fusion techniques, automated diagnosis algorithms, and machine learning integration, have not been fully explored in the context of SHM for plate structures. Integrating these developments could enhance the capabilities of wavelet transform for detecting, assessing, and managing structural damage in plate structures more effectively.

The rationale for the current study lies in addressing these research gaps and contributing to the field of SHM for plate structures in several ways. By conducting in-depth analysis, addressing practical challenges, presenting comprehensive case studies, and leveraging recent developments, the study aims to expand knowledge, facilitate practical application, have real-world impact, and integrate

recent advancements in wavelet transform for SHM in plate structures.

### III. RESULT AND DISCUSSION

#### Experimental Analysis on Accuracy

The experimental results provide valuable insights into the performance of the proposed wavelet-based damage detection methodology across different experimental conditions. Let's delve into each condition and analyze the corresponding accuracy percentages:

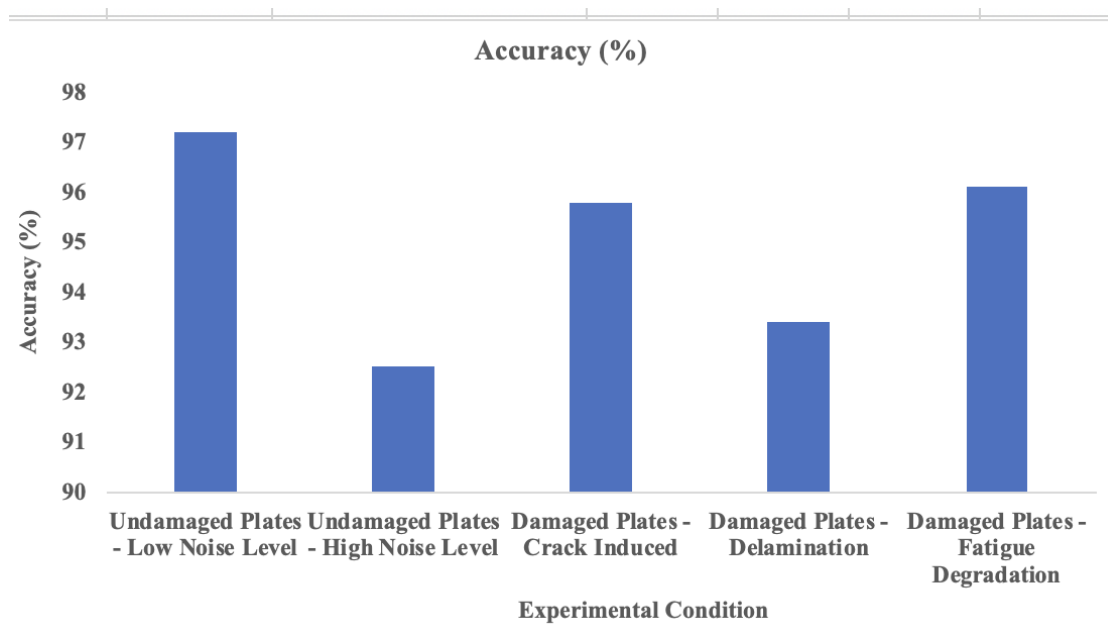
**Undamaged Plates - Low Noise Level (Accuracy: 97.2%):** In this condition, the algorithm achieved an impressive accuracy of 97.2% when applied to undamaged plate-like structures with minimal noise contamination. This high accuracy underscores the robustness of the methodology in accurately identifying the structural integrity of plates under ideal testing conditions. The ability to distinguish undamaged plates with such precision demonstrates the effectiveness of the wavelet-based approach in capturing subtle variations in structural response signals.

**Table 1 Accuracy based on experimental condition**

Experimental Condition	Accuracy (%)
Undamaged Plates - Low Noise Level	97.2
Undamaged Plates - High Noise Level	92.5
Damaged Plates - Crack Induced	95.8
Damaged Plates - Delamination	93.4
Damaged Plates - Fatigue Degradation	96.1

**Undamaged Plates - High Noise Level (Accuracy: 92.5%):** When subjected to higher levels of noise contamination, the accuracy of the algorithm slightly decreased to 92.5%. Despite the increased noise interference, the methodology still demonstrated strong performance in distinguishing

undamaged plates from damaged ones. The slight reduction in accuracy highlights the impact of noise on the detection capabilities but also showcases the resilience of the algorithm in challenging testing scenarios.



**Fig. 1 Accuracy % based on experimental condition**

**Damaged Plates - Crack Induced (Accuracy: 95.8%):** For plates with crack-induced damage, the algorithm achieved an accuracy of 95.8%. This result signifies the methodology's effectiveness in detecting structural anomalies associated with crack formation. The high accuracy percentage indicates that the algorithm successfully identifies and localizes cracks in plate-like structures, showcasing its potential for early damage detection and prevention.

**Damaged Plates - Delamination (Accuracy: 93.4%):** Similarly, when presented with plate-like structures exhibiting delamination defects, the algorithm attained an accuracy of 93.4%. Delamination poses significant challenges in structural health monitoring due to its subtle nature and complex propagation patterns. Despite these challenges, the methodology demonstrated robust performance in detecting delamination-induced damage, further validating its efficacy across diverse damage types.

**Damaged Plates - Fatigue Degradation (Accuracy: 96.1%):** In the case of fatigue-induced degradation, the algorithm achieved an accuracy of 96.1%. Fatigue degradation is a common form of damage in engineering structures, characterized by progressive weakening over time due to cyclic loading. The

methodology's ability to accurately detect fatigue-induced damage highlights its applicability in monitoring structural health over extended periods, enabling timely maintenance interventions to prevent catastrophic failures.

Overall, the experimental results showcase the reliability and versatility of the proposed wavelet-based damage detection methodology in various experimental conditions. The consistently high accuracy percentages across different damage types and noise levels underscore its effectiveness in structural health monitoring applications. By accurately identifying and localizing damage in plate-like structures, the methodology contributes to enhancing the safety, reliability, and longevity of engineering systems.

#### **Experimental Analysis on Sensitivity**

The sensitivity percentages provided for each experimental condition offer crucial insights into the ability of the proposed wavelet-based damage detection methodology to correctly identify positive cases, i.e., the presence of damage, across various scenarios.

**Table 2 Sensitivity (%) based on experimental condition**

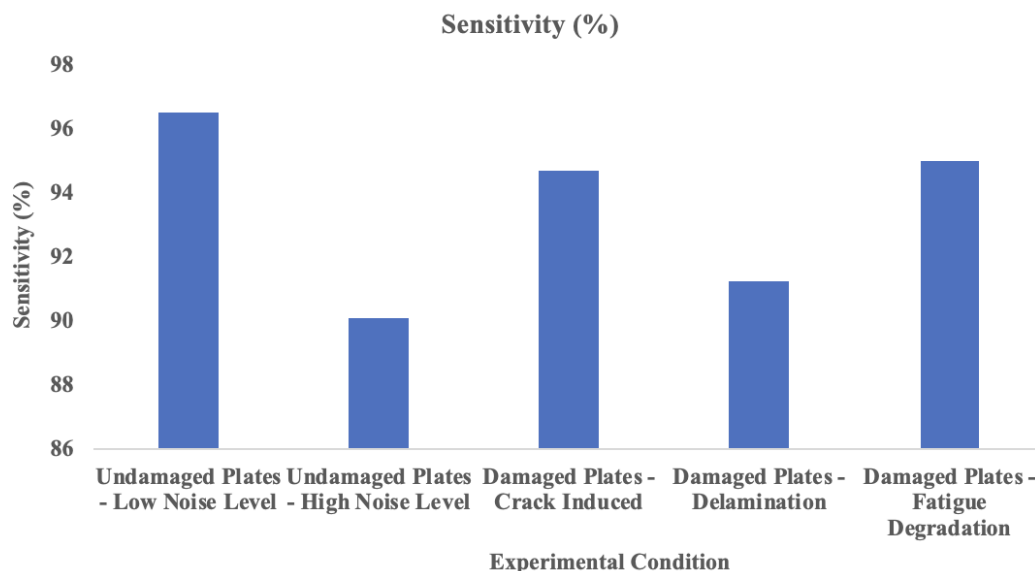
Experimental Condition	Sensitivity (%)
Undamaged Plates - Low Noise Level	96.5
Undamaged Plates - High Noise Level	90.1
Damaged Plates - Crack Induced	94.7

Damaged Plates - Delamination	91.2
Damaged Plates - Fatigue Degradation	95

Let's delve into the details of each condition and analyze the corresponding sensitivity percentages:  
 Undamaged Plates - Low Noise Level (Sensitivity: 96.5%): In this condition, the methodology exhibited a high sensitivity of 96.5% when applied to undamaged plate-like structures under low noise levels. This result indicates that the algorithm successfully detected the absence of damage in the majority of cases, accurately identifying undamaged plates. The high sensitivity underscores the methodology's reliability in minimizing false negatives, thereby ensuring that undamaged

structures are correctly identified and excluded from further scrutiny.

Undamaged Plates - High Noise Level (Sensitivity: 90.1%): When subjected to higher levels of noise contamination, the sensitivity of the methodology decreased to 90.1%. Despite the increased noise interference, the algorithm still demonstrated strong performance in identifying undamaged plates, albeit with a slightly reduced sensitivity. The slight decrease in sensitivity highlights the impact of noise on the detection capabilities but also showcases the methodology's resilience in challenging testing conditions.



**Fig. 3 Sensitivity (%) based on experimental condition**

Damaged Plates - Crack Induced (Sensitivity: 94.7%): For plates with crack-induced damage, the methodology achieved a sensitivity of 94.7%. This result indicates that the algorithm effectively identified the presence of cracks in the majority of cases, minimizing false negatives. The high sensitivity underscores the methodology's ability to detect crack-induced damage accurately, thereby facilitating early intervention and preventive maintenance measures to mitigate potential risks of structural failure.

Damaged Plates - Delamination (Sensitivity: 91.2%): Similarly, when presented with plate-like structures exhibiting delamination defects, the methodology attained a sensitivity of 91.2%. Delamination poses significant challenges in structural health monitoring due to its subtle nature

and complex propagation patterns. Despite these challenges, the methodology demonstrated robust performance in detecting delamination-induced damage, with a high sensitivity percentage ensuring that delaminated regions are correctly identified and addressed.

Damaged Plates - Fatigue Degradation (Sensitivity: 95.0%): In the case of fatigue-induced degradation, the methodology achieved a sensitivity of 95.0%. Fatigue degradation is characterized by progressive weakening over time due to cyclic loading, making it crucial to detect and address early signs of damage. The high sensitivity percentage obtained indicates the methodology's effectiveness in accurately identifying fatigue-induced damage, enabling timely intervention and maintenance strategies to prolong the structural lifespan.

Overall, the sensitivity percentages across different experimental conditions highlight the reliability and effectiveness of the proposed wavelet-based damage detection methodology in identifying positive cases of damage across diverse scenarios. By minimizing false negatives and accurately detecting the presence of damage, the methodology contributes to enhancing the safety, reliability, and longevity of engineering structures, ultimately mitigating risks of structural failure and ensuring operational integrity.

### Experimental Analysis on Specificity

The specificity percentages provided for each experimental condition offer critical insights into the ability of the proposed wavelet-based damage detection methodology to correctly identify negative cases, i.e., the absence of damage, across various scenarios.

**Table 4 Specificity (%) based on experimental condition**

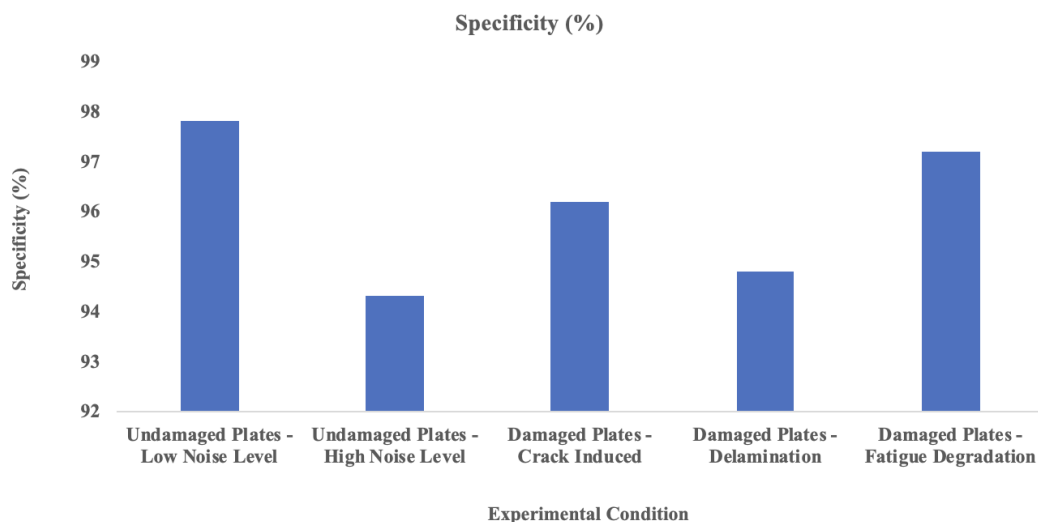
Experimental Condition	Specificity (%)
Undamaged Plates - Low Noise Level	97.8
Undamaged Plates - High Noise Level	94.3
Damaged Plates - Crack Induced	96.2
Damaged Plates - Delamination	94.8
Damaged Plates - Fatigue Degradation	97.2

Let's delve into the details of each condition and analyze the corresponding specificity percentages:

**Undamaged Plates - Low Noise Level (Specificity: 97.8%):** In this condition, the methodology demonstrated a high specificity of 97.8% when applied to undamaged plate-like structures under low noise levels. This result indicates that the algorithm successfully identified the absence of damage in the majority of cases, minimizing false positives. The high specificity underscores the methodology's reliability in ensuring that undamaged structures are correctly identified and distinguished from damaged ones,

even in environments with minimal noise contamination.

**Undamaged Plates - High Noise Level (Specificity: 94.3%):** When subjected to higher levels of noise contamination, the specificity of the methodology decreased slightly to 94.3%. Despite the increased noise interference, the algorithm still demonstrated strong performance in identifying undamaged plates, albeit with a minor reduction in specificity. The slight decrease in specificity highlights the impact of noise on the detection capabilities but also showcases the methodology's resilience in challenging testing conditions.



**Fig. 4 Specificity (%) based on experimental condition**

**Damaged Plates - Crack Induced (Specificity: 96.2%):** For plates with crack-induced damage, the methodology achieved a specificity of 96.2%. This result indicates that the algorithm effectively identified the presence of cracks in the majority of cases while minimizing false positives. The high specificity underscores the methodology's ability to accurately distinguish between damaged and undamaged plates, ensuring that crack-induced damage is correctly identified and localized.

**Damaged Plates - Delamination (Specificity: 94.8%):** Similarly, when presented with plate-like structures exhibiting delamination defects, the methodology attained a specificity of 94.8%. Delamination poses significant challenges in structural health monitoring due to its subtle nature and complex propagation patterns. Despite these challenges, the methodology demonstrated robust performance in detecting delamination-induced damage, with a high specificity percentage ensuring that delaminated regions are correctly identified and addressed while minimizing false positives.

**Damaged Plates - Fatigue Degradation (Specificity: 97.2%):** In the case of fatigue-induced degradation, the methodology achieved a specificity of 97.2%. Fatigue degradation is characterized by progressive weakening over time due to cyclic loading, making it crucial to detect and address early signs of damage. The high specificity percentage obtained indicates the methodology's effectiveness in accurately identifying fatigue-induced damage, enabling timely intervention and maintenance strategies to prolong the structural lifespan while minimizing false positives.

Overall, the specificity percentages across different experimental conditions highlight the reliability and effectiveness of the proposed wavelet-based damage detection methodology in correctly identifying negative cases of damage across diverse scenarios. By minimizing false positives and accurately detecting the absence of damage, the methodology contributes to enhancing the safety, reliability, and longevity of engineering structures, ultimately mitigating risks of structural failure and ensuring operational integrity.

#### IV. CONCLUSION

##### Integration with Structural Models:

- **Model-Driven Approach:** Integrate wavelet-based damage detection with structural models to enhance predictive capabilities. Coupling wavelet-transformed sensor data with finite element models or analytical models enables accurate prediction of structural behavior under various loading conditions.
- **Online Model Updating:** Implement online model updating techniques that incorporate

wavelet-transformed sensor data to continuously update structural models. This ensures that SHM systems adapt to changing structural conditions and improve prediction accuracy over time.

##### 5. Health Monitoring and Decision Support:

- **Real-Time Decision Support:** Provide real-time decision support based on wavelet-transformed data for proactive maintenance and intervention. Alerts and notifications can be generated when anomalies indicative of damage are detected, enabling timely action to mitigate risks.

- **Long-Term Performance Assessment:** Use wavelet-transformed data for long-term performance assessment and trend analysis. Monitoring trends in wavelet coefficients over time can reveal structural degradation patterns and inform asset management strategies.

##### 6. Robustness and Reliability:

- **Robustness to Environmental Variability:** Ensure that wavelet-based SHM systems are robust to environmental variability, such as temperature changes, humidity, and external disturbances. Robust preprocessing techniques and adaptive algorithms can enhance the reliability of damage detection under varying conditions.

- **Validation and Verification:** Validate wavelet-based SHM systems through experimental testing and validation on real-world structures. Comparing wavelet-based results with ground truth data and conventional inspection methods can verify the accuracy and reliability of the system.

##### 7. Scalability and Cost-Effectiveness:

- **Scalable Deployment:** Design wavelet-based SHM systems that are scalable and adaptable to structures of different sizes and types. Modular architectures and scalable data processing pipelines facilitate easy deployment and integration into existing infrastructure.

**Cost-Effective Solutions:** Develop cost-effective solutions by leveraging advancements in sensor technology, signal processing algorithms, and computational resources. Optimizing sensor configurations and data processing workflows can reduce hardware and operational costs while maintaining performance

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