N.M.Sai Krishna Kumar, K.Steven / International Journal of Engineering Research and Applications (IJERA) ISSN: 2248-9622 www.ijera.com Vol. 2, Issue4, July-August 2012, pp.1566-1571 Performance Analysis Of Bluetooth System Using Optimized Differential GFSK Demodulator

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Abstract

In this project, a simple demodulator for GFSK receivers is developed, which averages the phase based on the signal-to-noise ratio (SNR) maximizing criterion, and does not require knowledge of the exact modulation index. Compared to demodulators with similar complexity, such as the LDI, the presented receiver can achieve superior performance. In digital modulation, Gaussian frequency shift keying(GFSK) is one of the shifting technique. we are facing a challenging task in simple and high performance receivers for GFSK. In our project we develop an optimized differential GFSK demodulator and investigate the phase wrapping issue in its implementation. The Experimental results shows performance of bit error rate improvement in with conventional differential demodulators in both AWGN and flat fading channels. We also compare the simulation results with other exiting techniques like fading channels.

Keywords Gaussian frequency shift keying (GFSK), differential demodulation, phase wrapping.

I. INTRODUCTION

Gaussian Frequency-Shift Keying (GFSK) is a type of Frequency Shift Keying modulation that uses a Gaussian filter to smooth positive/negative frequency deviations, which represent a binary 1 or 0. It is used by DECT, Bluetooth. Bluetooth is a proprietary open wireless technology standard for exchanging data over short distances (using shortwavelength radio transmissions in the ISM band from 2400–2480 MHz) from fixed and mobile devices, creating personal area networks (PANs) with high levels of security. Created by telecoms vendor Ericsson in 1994, it was originally conceived as a wireless alternative to RS-232 data cables. It can connect several devices, overcoming problems of synchronization.

Bluetooth is managed by the Bluetooth Special Interest Group, which has more than 16,000 member companies in the areas of telecommunication, computing, networking, and consumer electronics. The SIG oversees the

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development of the specification, manages the qualification program, and protects the trademarks. To be marketed as a Bluetooth device, it must be qualified to standards defined by the SIG. A network of patents is required to implement the technology and are licensed only for those qualifying devices; thus the protocol, whilst open, may be regarded as proprietary. GFSK is an important digital modulation scheme. It is widely used in low cost and low power consumption systems such as Bluetooth in the unlicensed 2.4 GHz industrial, scientific and medical (ISM) band due to its spectral efficiency, constant signal envelope property and the possibility for low complexity receivers. The optimum GFSK receiver consists of a correlator followed by a maximumlikelihood sequence detector that searches for the minimum Euclidean distance path through the state trellis based on Viterbi algorithm.

However, due to the complexity of the matched filter bank and carrier synchronization, such a receiver has very limited applications. In addition, these designs always assume a certain nominal value for the modulation index h. However, the modulation index may vary in a relatively wide range (for Bluetooth, the modulation index is allowed to vary between 0.28 and 0.35), leading to a varying trellis structure for sequence detection with possibly tremendous number of states. All these render this optimum receiver impractical.

Hence non-coherent suboptimal receivers are typically preferred, especially in systems where it is desirable to have a simpler receiver structure. The technique phase wrapping shown is successful provided that the true gradient is bounded to $< \pi$. It is unlikely so when both the sampled topography is rough and elevations are $> \Delta$ Hamb. Slow varying topographies are not a problem even if elevations are large. Rough topographies are not a problem if elevations are contained. We adopt a highperformance GFSK receiver that achieves near optimum performance in AWGN [1] but uses a prohibitively complex bank of filters to match a large set of legitimate waveforms over several bit intervals. However, we reduce the computational cost by

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performing filtering over a single bit interval, and propagating the results over successive bit periods, thereby eliminating redundancy in providing the matched filter outputs. We also propose a blind algorithm for carrier frequency correction. It is based on the observation of the phase gain in the transmit signal over a finite time-interval. Our derivation concurs with work by other researchers [7].

II. GFSK SIGNAL MODEL

A pass-band transmitted GFSK signal can be represented as

$$s(t,\alpha) = \sqrt{\frac{2E_b}{T}} \cos \left[2\pi f_0 t + \varphi(t,\alpha) + \varphi_0 \right]$$

Where E_b is the energy per bit, T is the symbol period, f_0 is the carrier frequency, $_0$ is an arbitrary constant phase shift. The output phase deviation (t,) is determined by the input data sequence $\alpha = ..., \alpha_{-2}, \alpha_{-1}, \alpha_0, \alpha_1, \alpha_2$, with $\alpha_i \in +/-1$.

$$\varphi(t,\alpha) = 2\pi h \sum_{i=n-L+1}^{n} \alpha_i q(t-iT) + \pi h \sum_{i=-\infty}^{n-L} \alpha_i$$
(2)

Where h is the modulation index

$$q(t) = \int_{-\infty}^{t} g(T) dT \text{ . With}$$

$$g(t) = Q\left(\gamma.BT\left(\frac{t}{T} - \frac{1}{2}\right)\right) - Q\left(\gamma.BT\left(\frac{t}{T} + \frac{1}{2}\right)\right), \quad (3)$$

Being the frequency pulse with constant $\gamma = 2\pi/\sqrt{(\ln(2))}$ and Q(x) is the Gaussian Q-function. BT is the 3 dB bandwidth-time product. Generally speaking, the smaller the BT values, the more significant the ISI introduced due to the increase of the effective frequency pulse duration. In the Bluetooth standard, h can vary between 0.28 and 0.35 and BT equals 0.5 with T = 10-6s, giving rise to a (t) with effective duration of 2T.

A. Baseband Equivalent System Model:

The channel model considered is Rayleigh flat fading with additive white Gaussian noise (AWGN). The received signal is first passed through a receiver filter with transfer function (f), then the phase differential detection is performed on the output signal of the filter. The input signal to the receiver filter is

$$\bar{\mathbf{r}}(\mathbf{t}) = e^{j\theta(t)}h(t) * s_l(t) + n(t)$$
(4)

 $h0 \sim C\mathcal{N}(0, 1)$, n(t) is zero mean white Gaussian noise with single-sided spectral density N0, and sl(t) is the complex envelope of the GFSK transmitted signal $\theta(t)$ is the time-varying channel phase, h(t) is the channel impulse response.

$$s_{l}(t) = \rho \exp\left[j(\varphi(t,\alpha) + \varphi_{0})\right]_{(5)}$$

We assume that the receiver filter has sufficient band width such that it will introduce negligible distortion on the signal while band limiting the noise. Thus the output of the receiver filter is

$$r(t) = e^{j\theta(t)}h(t) * s_l(t) + \eta(t)$$

Where $(t) = (t) + j\eta i(t)$ is band limited zero mean Gaussian noise with autocorrelation

$$R_{\eta}(T) = N_0 \int_{-\infty}^{\infty} \left| \boldsymbol{H}_r(f) \right|^2 \exp(j 2\pi f_T) df,$$

(7) And average power

$$P_{\eta} = R_{\eta}(0) = N_0 \int_{-\infty}^{\infty} \left| H_r(f) \right|^2 df \Delta N_0 B_n$$

(8)

Where Bn is the equivalent noise bandwidth of the receiver filter. We assume that (t) does not change over a symbol period. For the phase differential demodulation, we take the difference of consecutive phase samples; the unknown phase is thus canceled. In addition, ηr and ηi are independent and each has a distribution of $(0, \sigma 2)$, where the variance $\sigma 2$ is defined as $\sigma 2 = (0) = NOBn$. Hence the joint distribution of ηr and is

$$f_{\eta_r \eta_i}(x, y) = \frac{1}{2\pi\sigma^2} e^{-\frac{x^2 + y^2}{2\sigma^2}}$$

III. OPTIMIZED GFSK DEMODULATOR

In this section, we first present the basic ideas of conventional phase differential demodulation. To facilitate the design of our optimized differential demodulator, the phase noise distribution is then derived. Based on the phase noise distribution, we will then propose an optimized differential demodulator and investigate the phase wrapping problem.

A. Differential GFSK Demodulation;

In this subsection, we consider the basic ideas about differential demodulation in AWGN. For Bluetooth standard, the effective frequency pulse

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duration is 2*T*, giving rise to a piecewise monotonic phase trellis within each symbol duration. The direction of the monotonic change is determined by the binary symbol value. Hence, a phase differential demodulator can be employed. We first extract the phase of the received signal.

$$\phi(t) = \angle r(t) = \varphi(t) + \phi_{\eta}(t)$$
⁽¹⁰⁾

Where φ (*t*) is determined by the transmitted phase and (*t*) is a random variable due to the AWGN. Essentially, the conventional differential demodulator involves sampling (*t*) in (9) at symbol rate to obtain () and then taking the difference of the neighboring samples.

$$\Delta \phi(nT) = \phi(nT) - \phi(nT - T)$$
(11)

A decision can then be made based on the sign of $\Delta(nT)$. However, due to the randomness of the phase noise, the decision based on a single phase sample per symbol lacks sufficient reliability so that conventional differential demodulator suffers from degraded performance. Intuitively, one can average a portion of every symbol long trellis segment instead of a single sample at each end before taking the difference. This may provide some gain in the signalto-noise ratio (SNR). In the case of Gaussian noise, the gain in SNR leads to improvement in BER. To facilitate the design of an optimum differential demodulator, we will next study the distribution of phase noise (t). For the simplification of analysis, we will first consider the AWGN channel. The result can then be easily extended to flat fading channels.

B. Phase Noise Distribution:

For notational simplicity, let (t) = 0 in (9) without loss of generality. It then follows that (t) = (t). Denote the probability density function (PDF) and the cumulative density function (CDF) of the random variable (t) as (φ) and (φ) , respectively. We first consider $0 \le (t) \le \pi/2$, on which.

$$F_{\phi}(\varphi) = P_r(0 \le \phi \le \varphi)$$
$$= \int_{-\rho}^{\infty} \int_{0}^{(\rho+x)\tan\varphi} f_{\eta r \eta i}(x, y) dy dx.$$

(12)

Then by Leibnitz's rule, the PDF is derived as $f_{\phi}(\varphi) = \frac{d}{d\varphi} F_{\phi}(\varphi)$

$$=\frac{1}{2\pi\sigma^2}\int_{-\rho}^{\infty}e^{-\frac{x^2+(\rho+x)^2\tan^2\varphi}{2\sigma^2}}\frac{d}{d\varphi}[(\rho+x)\tan\varphi]dx$$

$$=\frac{1}{2\pi}e^{-\frac{\rho^2}{2\sigma^2}}+\frac{\rho\cos\varphi}{\sqrt{2\pi\sigma}}e^{-\frac{\rho^2\sin^2\varphi}{2\sigma^2}Q\left(-\frac{\rho\cos\varphi}{\sigma}\right)}$$

(14)

For $\pi/2 < (t) < 2\pi$, only the integral interval in (10)is slightly different for each quadrant, and it can be readily shown that the final PDF results are the same as (11) for all(*t*)values. At high SNR (large ρ), we have exp ($-\rho 2 \ 2\sigma 2$) \approx 0and $Q(-\rho \cos\phi\sigma) \approx 1$. As a result, the complicated noise distribution can be approximated as:

$$f_{\phi}(\varphi) \approx \frac{1}{\sqrt{2\pi\sigma/\rho}} \cdot e^{-\frac{1}{2} \cdot \frac{\varphi^2}{(\sigma/\rho)^2}}$$
(1)

5)

Which is simply the Gaussian distribution with zero mean and variance $(\sigma/\rho)^2$. Such a Gaussian approximation of the phase noise distribution can be very useful if the approximation is accurate. This is because our demodulator design is intended to optimize the ultimate BER performance of the system. In the case of Gaussian noise, minimizing BER is equivalent to maximizing the SNR, leading to a readily-achievable SNR maximizing system optimization criterion. This is generally not true for non-Gaussian noise. In order to assess the accuracy of our approximation; we perform two sets of simulations. In the first simulation, we compare the true and approximate PDF curves at various SNR values. As below shown in Figure 1, we observe that these curves are already very close at $\rho 2/(2\sigma 2) = 2$ dB, and are nearly identical at $\rho 2/(2\sigma 2) = 8$ dB. We also simulate and compare the BER performance of a simple binary system where the additive noise follows either the true noise PDF or the Gaussian approximation. The result in Below Figure. 2 shows that the BER performances of the two are very similar. You may note that the BER gap at higher SNR seems to be larger than the gap at lower SNR. However, since the scale is different in the BER axis, the approximation is actually much better at higher SNR, which confirms our previous analysis .So far, we have verified that the noise in the extracted phase can be well approximated as Gaussian distributed. With all the knowledge above, we will develop our optimized differential GFSK demodulator in the following subsection.

C. Optimized Differential GFSK Demodulator:

Each symbol-long phase trellis segment can take one of the four shapes depending on the specific

(13)

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symbol sequence. For example, for an input data sequence of (1,-1, 1,-1, 1, 1, 1, 1),



Figure 1: PDF curves for $\rho/(\sigma) = 0.2828$ and $\rho/(\sigma) = 0.6083$

phase trellis during [0, T) is linear in the first half and nonlinear in the second half (which we term as type D); the phase trellis during [T, 2T) is nonlinear throughout the entire duration (which we term as type C); the phase trellis during [4T, 5T) is nonlinear in the first half and



Figure 2: BER performance for the exact phase noise and the approximated Gaussian phase noise

linear in the second half (which we term as type *B*); and the phase trellis during [5T, 6T) is linear throughout (which we term as type *A*). Without loss of generality, we will start from the linear phase segment and then generalize to the nonlinear and partly nonlinear ones. A linear phase curve segment has a function $(t) = A \cdot t/T$, $t \in [0,)$. Note that the scalar *A* is proportional to the modulation index *h*. However, since its value does not affect the optimization result, we will normalize it to 1 for notational simplicity (the same for the nonlinear phase curve cases). Let *T* obe the portion at each end of this segment over which we average before taking the difference, as illustrated in Then the resultant SNR is:

$$SNR_{A}(T_{0}) = \frac{\left(\int_{T-T_{0}}^{T} \frac{t}{T} dt - \int_{0}^{T} \frac{t}{T} dt\right)^{2}}{2T_{0}\sigma^{2}}$$

(16)

(18)

As we have shown in the preceding subsection, the phase noise can be well approximated as Gaussian distributed even at fairly low SNR. Hence, the SNR-maximizing *To* is essentially also BER-minimizing. Maximizing SNR_A for a given symbol duration *T* and $A2/\sigma 2$, we obtain

$$\max_{0 \le T_0 \le T/2} SNR_A(T_0) = \max_{0 \le T_0 \le T/2} \frac{T_0(T - T_0)^2}{2T^2 \sigma^2},$$
(17)

Which results in To=T/3. This indicates that one should average the first and last 33% of each symbol-long phase segment and then take their difference on which a decision can be made. Next we consider the type-C phase segment during [T, 2). The exact function for this segment does not have a closed form (containing the integral of Gaussian Q function). How ever we notice that each half of the segment curves in the shape of parabola approximately. Hence we use two second-order polynomials to fit each half; that is x1(t) = -0.9202(t/T)2 - 0.1797(t/T) + 0.8158, $t \in [0, 0.5T)$, and x2(t) = 0.9202(t/T)2 - 1.9911(t/T) + $1.273, t \in [0.5T,T)$. Accordingly, the resultant SNR after averaging and difference taking is:

$$SNR_{c}(T_{0}) = \frac{\begin{pmatrix} T & T_{0} \\ \int x_{2}(t)dt - \int x_{1}(t)dt \\ T - T_{0} & 0 \end{pmatrix}^{2}}{2T_{0}\sigma^{2}}$$

As a result, the optimal portion should be chosen as To=0.3675.Similar results can be obtained for type-B and type-D phase segments. Due to the space limit, these are omitted here. Since the four different shapes occur with equal probability, one can also find the overall optimum T_o by solving

$\max_{0 \le T_0 \le T/2} \left[SNR_A(T_0) + SNR_B(T_0) + SNR_C(T_0) + SNR_D(T_0) \right],$ (19)

which results in To=0.35T. The continuoustime analysis can be readily extended to the discretetime sampled phase segments. Let 2K denote the number of samples per symbol. The problem now is to determine the optimum M, which is the number of samples to be averaged at each end of the 2Ksamples per symbol. Denote the second group of Msamples as S1, ..., SM,

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Figure 3: Cumulative Distribution Function

and the first group of *M*samples as S'1, ..., S'M. It then follows that $Si = (K-1 + i)/(2K-1) + \eta i$ and S' $i = (i-1)/(2K-1) + \eta' i$, i = 1, ..., M. Consider again the type-A linear phase segment. With the Gaussian approximation of the phase noise, the difference between the two averages is ΣM i=1(Si-S'i)/M, leading to an SNR of

$$SNR_{A}^{(d)}(M) = \frac{M(2K-M)^{2}}{2(2K-1)^{2}\sigma^{2}},$$
20)

Where superscript (a) indicates discretetime. Clearly, SNR(d A(M)) bears a form very similar to SNR(To) in (13).Not surprisingly, maximizing SNR (d) A(M) results in M=2K/3, which agrees perfectly with the continuous-time result. Using the same methodology, we can obtain the optimum *M* for the general case as M = 0.7K. Thus, by choosing the optimal M, the SNR is maximized and the error probability minimized. The block diagram of our optimized differential demodulator is shown in Fig. 4. We can see that the only difference between this new demodulator and the conventional differential one is the averaging part. To evaluate the performance gain by using the optimized differential demodulator, we notice that the conventional differential demodulator can be considered as a special case with M=1 for any Kvalues. Considering again the type-A phase segment, and evaluating(17) at M = 2K/3 and M =1 and taking the relative ratio, we obtain the SNR gain over conventional differential demodulator as:

$$\frac{SNR_{A}^{(d)}(2K_{3})}{SNR_{A}^{(d)}} = \frac{32}{27}\frac{K^{3}}{27(2K-1)^{2}}.$$

This gain is a function of because the optimum number of averaged samples M is dependent on the total number of available samples 2K. The above

results can be readily extended to the flat fading channels since each realization of the channel fading coefficient is essentially an AWGN case. All these results will be verified by simulations.

D. Phase Wrapping Problem:

When realizing these phase differential demodulation algorithms, however, there is an implementation problem. Recall that our differential operations are performed on the phase function (t) in (9). Unlike the original phase trellis (t,) in (2), (t) is not only noisy, but also suffers from the phase wrapping problem since it assumes a finite range of 2π . To solve this problem, conventional differential demodulator in takes the following structure: the received signal (t) is multiplied by a T-delayed and $\pi/2$ phase-shifted version of itself and then sampled at the symbol rate to give the decision statistic. These operations will essentially give $sin[\Delta(nT)]$ without explicitly extracting $\phi(t)$, thus avoiding the phase wrapping problem. Since the decision only relies on the sign of $\Delta(nT)$, the above operations leading to $\sin[\Delta\phi(nT)]$ generally preserves this sign information. However, for large modulation index $h \ge 1$, the phase change $\Delta(nT)$ over one symbol duration may exceed π . In this case, the sin operator cannot preserve the sign of $\Delta(nT)$ any more. Hence, in both the conventional and optimized differential demodulators, we directly deal with the phase extracted from the received signal. Specifically, the phase is unwrapped by simply adding 2π when the absolute change between the Consecutive phase samples is greater than the jump tolerance π . Both methods are tested and compared by simulations.



Figure 4 BER Performance in AWGN Channel

We will evaluate the performance of our proposed demodulator by simulations in terms of BER versus Eb/N0, where Eb is the signal energy per information bit and N0 is the power spectral density of the additive noise. In all simulations, we set BT=

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0.5, BnT = 1 and take 8 samples per symbol. Show the BER performance of our optimized differential demodulator together with that of the conventional one and the LDI demodulator with different modulation indices h in AWGN and flat fading channels, respectively. In particular, for the conventional differential demodulator, we simulated both the system in which avoids phase wrapping as well as our direct unwrapping approach. We observe that, the optimized demodulator shows about $1 \sim 2 \text{ dB}$ improvement over the conventional differential receivers and the LDI especially at high SNR. Note that, for small h(h=0.33 or 0.5), phase unwrapping does not lead to any performance improvement in the conventional receiver. This confirms that the performance gain is entirely due to our optimized demodulation algorithm. This result is also consistent with the theoretical result obtained in with K=4. Note that the complexity of LDI is similar to the optimized demodulator since LDI also needs oversampling. In addition, in both cases, as h increases.





Performances of all demodulators except the conventional scheme without phase unwrapping in improve accordingly. We note that when h=1, the conventional differential demodulator in suffers from significant performance loss. This is because the phase change during one symbol interval may exceed π for large h(h=1) such that the sin operator cannot preserve the sign of $\Delta(nT)$ anymore. In addition, the gain of the optimized demodulator over the conventional one for large h is not as significant as that for small h. This is due to the phase unwrapping operation. As h increases, the phase change over one symbol interval will increase. However, the error introduced to the recovered phase by phase un wrapping operation will also increase. Therefore the BER performance improvement is not a strictly increasing function of the modulation index h.

V. CONCLUSION

In this project the operation of GFSK demodulator in Bluetooth radio signals is explained.

Simulation results coincides with the concept of GFSk distribution (PDF) employed in Bluetooth which is simply the gaussin distribution with zero mean and variance $(\sigma/\rho)^2$. The simulation results of BER (Bit Error Rate) performance of a simply binary system using DPSK are compared where the additive noise follows the true noise PDF as this basic demodulator designed is intended to optimize the ultimate BER performance of the system.

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