

## Advances in Energy Detector and a Matched Filter based Spectrum Sensing: A Survey

Yogesh Patidar\*, Prof. Kuldeep Pandey\*\*

\* (Department of Electronics and Communication Engg, BCE RKDF University, Bhopal

\*\* (Asst. Prof., Department of Electronics and Communication Engg, BCE RKDF University, Bhopal

\* Corresponding Author: Yogesh Patidar

### ABSTRACT

The electromagnetic spectrum, licensed to use by governments, is a limited natural resource. The concept of cognitive radio networks (CRNs) has evolved in past few decades and recently implemented in some areas of wireless communication, namely IEEE 802.11af, IEEE 802.15.4m, ECMA 392 and IEEE 802.22, as a technique to use underutilized spectrum. The key development areas in CRNs are spectrum sensing and monitoring, spectrum analysis, spectrum mobility and spectrum decision. Research articles have classified Spectrum sensing as narrowband and wideband spectrum sensing. This paper presents the fundamentals of narrowband spectrum sensing and reviews the implementation and challenges associated with energy detector (ED) and a matched filter (MF) based spectrum sensing.

**Keywords**-Cognitive radio networks, energy detector, matched filter, probability of detection, probability of false alarm, probability of miss detection, receiver operating characteristics

### I. INTRODUCTION

The Federal Communications Commission's (FCC's), the federal agency responsible for implementing and enforcing America's communications law and regulations, similar to Telecom Regulatory Authority of India (TRAI) in India, spectrum use measurement reveals that some spectrum bands are underutilized at different times in different geographic locations [1]. In static spectrum allocation fixed channels are assigned to users known as a licensed user or Primary Users (PU). When such PU is not present at a specific time the allocated spectrum band remain free and results in underutilization of spectrum bands as shown in figure 1. These free spectrum bands, for a particular time duration and at a specific geographic location, are called spectrum holes.

Cognitive Radio Networks (CRN) plays a vital role in improving spectrum efficiency. Cognitive radio (CR), as defined in [2], is an intelligent wireless communication system that senses and learn its surrounding radio environment and adapt its state to internal changes.

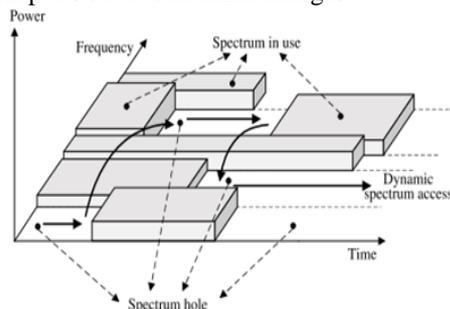


Fig.1: Spectrum hole [2]

In CRN's the unused spectrum is used opportunistically by the CR's, also known as Secondary Users (SU) or unlicensed users, temporarily without interfering the PU. The CRN's employ Dynamic Spectrum Allocation (DSA) for opportunistically using the underutilized spectrum. The DSA works on a cognitive cycle with spectrum sensing, spectrum analysis, spectrum mobility and spectrum sharing as four main phases[3]. In the spectrum sensing phase, CR finds the spectrum holes which then analyzed for suitability of transmission and assigned to SU in spectrum analysis phase. Meanwhile, the CR continuously sense the spectrum for new spectrum hole and presence of PU on its licensed band. As soon as PU appear on its licensed band, the spectrum mobility comes into play and assign new spectrum hole to SU and vacate the PU's licensed band. Spectrum sharing is all about coordination of available spectrum holes between all SU's.

In section II we have given a mathematical foundation for spectrum sensing which further applied to a matched filter based detection and energy detector in section III and section IV respectively. Section III and section IV also cover the research advancements and MATLAB simulation.

### II. SPECTRUM SENSING (SS)

The conventional definition of spectrum sensing is to detect unused spectrum bands or spectrum holes of PU's. The various aspects of spectrum sensing include sensing approaches, enabling or sensing algorithms, challenges,

cooperative sensing, multi-dimensional spectrum sensing and standards that employ sensing[4]. Researchers have classified Spectrum sensing algorithms as coherent and noncoherent algorithms. The coherent spectrum sensing algorithms, such as matched filter, require the prior information of PU whereas noncoherent algorithms, such as energy detector, investigate channel for spectrum holes without any prior information of PU. To explore further spectrum sensing techniques, we first present the mathematical framework and common terminologies used in energy detector and a matched filter based spectrum sensing. These techniques use the Neyman-Pearson (NP) approach for spectrum sensing [5]. Consider a simple binary hypothesis testing problem to choose one of the two hypotheses,  $\mathcal{H}_0$  and  $\mathcal{H}_1$ .

$$\mathcal{H}_0 : y[n] = w[n] \quad (\text{Noise only})$$

$$\mathcal{H}_1 : y[n] = x[n] + w[n] \quad (\text{Signal with noise})$$

Where  $\mathcal{H}_0$  is a null hypothesis which represents noise ( $w[n]$ ) only or absence of signal and  $\mathcal{H}_1$  is the alternative hypothesis which represents the presence of a signal ( $x[n]$ ) with noise ( $w[n]$ ). We assume that  $w[n]$  is White Gaussian Noise (WGN) which is zero-mean Gaussian noise process with autocorrelation function  $r_{ww}[k] = E(w[n]w[n+k]) = \sigma_w^2 \delta[k]$  where  $\delta[k]$  is a unit Dirac delta function. Now with  $x[n] = A$  (DC level), the probability density function (PDF) or the likelihood corresponding to the two hypotheses can be given as:

$$p(y[n]:\mathcal{H}_0) = \frac{1}{(2\pi\sigma_w^2)^{\frac{1}{2}}} e^{-\frac{(y[n])^2}{2\sigma_w^2}} \quad (1)$$

$$p(y[n]:\mathcal{H}_1) = \frac{1}{(2\pi\sigma_w^2)^{\frac{1}{2}}} e^{-\frac{(y[n]-A)^2}{2\sigma_w^2}} \quad (2)$$

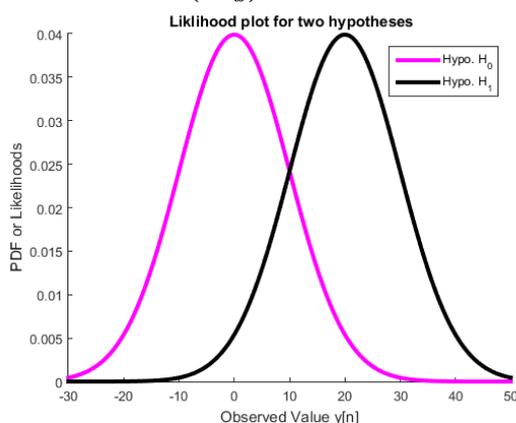


Figure 2: PDF or Likelihood plot for the two hypotheses

The Fig.2 gives a plot of two densities. According to observation  $y[n]$ , we choose  $\mathcal{H}_0$  if  $p(y[n]:\mathcal{H}_0) > p(y[n]:\mathcal{H}_1)$  and  $\mathcal{H}_1$  if  $p(y[n]:\mathcal{H}_0) \leq p(y[n]:\mathcal{H}_1)$ . These two conditions can be summarized as

Likelihood Ratio Test (LRT), where we choose  $\mathcal{H}_0$  if  $L(y) = \frac{p(y[n]:\mathcal{H}_1)}{p(y[n]:\mathcal{H}_0)} < 1$  and  $\mathcal{H}_1$  if  $L(y) = \frac{p(y[n]:\mathcal{H}_1)}{p(y[n]:\mathcal{H}_0)} \geq 1$ . LRT test for above given noise and signal statistics decide  $\mathcal{H}_0$  if  $y[n] < \frac{A}{2}$  and  $\mathcal{H}_1$  if  $y[n] \geq \frac{A}{2}$ . Fig.3 shows result of MATLAB simulation for a signal  $x[n] = 20$  and WGN with  $\sigma_w = 10$ . The value  $\frac{A}{2} = 10$  is a threshold of the detector. The area shown with horizontal green line gives the Probability of Detection ( $P_D$ ). In above detection process there are two types of possible errors: Type I error is area shaded with red lines where noise is present and we choose it as noise with signal. This is also known as Probability of False Alarm ( $P_{FA}$ ). Type II error is area shaded with Blue lines, where a signal with noise is present and we choose it as only noise. This is also known as Probability of Miss Detection ( $P_{MD}$ ). A good detector is one with maximum  $P_D$  and minimum  $P_{FA}$  but here we find a tradeoff between  $P_{FA}$  and  $P_D$ , hence we cannot minimize  $P_{FA}$  while we maximize  $P_D$ . NP theorem define LRT as an optimal detector which maximizes  $P_D$  for a given  $P_{FA} = \alpha$  where threshold  $\gamma$  is given by

$$P_{FA} = \int_{\{y[n]:L(y)>\gamma\}} p(y[n]:\mathcal{H}_0) dy = \alpha \quad (3)$$

The curve  $P_D$  versus  $P_{FA}$ , known as Receiver Operating Characteristics (ROC), gives the detection performance of a NP detector.

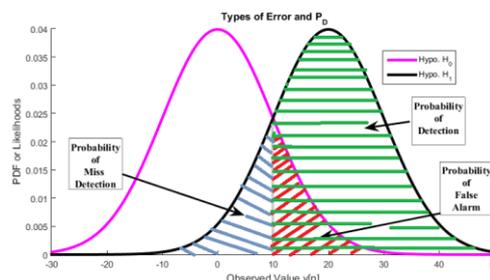


Figure 3: Types of error and  $P_D$

### III. MATCHED FILTER BASED SS

It is coherent spectrum sensing technique where prior information of PU is required to detect the presence of PU. For a known signal  $x[n]$ , and additive WGN  $w[n]$ , the likelihoods corresponding to the two hypotheses can be given as:

$$p(\bar{y}:\mathcal{H}_0) = \frac{1}{(2\pi\sigma_w^2)^{\frac{N}{2}}} e^{-\frac{\|\bar{y}\|^2}{2\sigma_w^2}} \quad (4)$$

$$p(\bar{y}:\mathcal{H}_1) = \frac{1}{(2\pi\sigma_w^2)^{\frac{N}{2}}} e^{-\frac{\|\bar{y}-\bar{x}\|^2}{2\sigma_w^2}} \quad (5)$$

Where  $\bar{y} = [y[0], y[1], y[2], \dots, \dots, y[N-1]]^T$  and  $N$  is the number of sample in an observation. The log LRT gives the test statistics:

$$T[Y] = \sum_{n=0}^{N-1} Y[n]x[n] = \bar{x}^T \bar{y} \quad (6)$$

As discussed in the previous section  $P_{FA}$  and  $P_D$  are calculated as:

$$P_{FA} = P_r\{T(Y) > \gamma'; \mathcal{H}_0\} = Q\left(\frac{\gamma'}{\sigma_\omega \|\bar{x}\|}\right) \quad (7)$$

$$P_D = P_r\{T(Y) > \gamma'; \mathcal{H}_1\} = Q\left(\frac{\gamma' - \|\bar{x}\|^2}{\sigma_\omega \|\bar{x}\|}\right) \quad (8)$$

From (7), we can calculate  $\gamma'$  for different values of  $P_{FA}$  (using NP theorem). Fig.4 shows the theoretical and MATLAB simulated  $P_D$  performance of matched filter detector for different values of SNR.

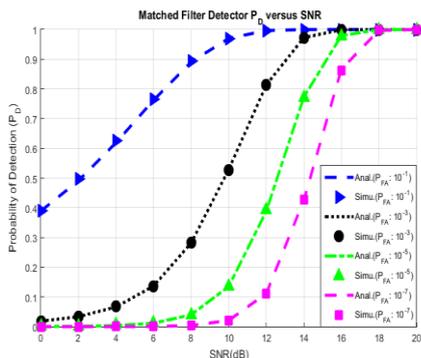


Figure 4: Matched filter detector  $P_D$  Vs. SNR

From (7) and (8), we get ROC as:

$$P_D = Q\left(Q^{-1}(P_{FA}) - \sqrt{\frac{\|\bar{x}\|^2}{\sigma_\omega^2}}\right) \quad (9)$$

In [6] it is proved that matched filter maximizes SNR and is an optimum for signal detection when the signal is known. In [7] PU's prior information requirement at physical and MAC layer is discussed with the issue of timing and carrier synchronization. In [8] a matched filter based validated MATLAB simulation is given to detect frequency modulated signals at 100 MHz, which meet the requirements of IEEE802.22 standards. In [9] robustness of coherent detectors is analyzed under uncertainty of physical systems. In [10] multiple thresholds based spectrum sensing is discussed where matched filter is used to detect PU with different power levels.

#### IV. ENERGY DETECTOR BASED SS

It is noncoherent spectrum sensing technique where PU is unknown (signal with an arbitrary covariance matrix) to SU. For simplicity, we consider a signal  $x[n]$ , a zero mean, white Gaussian random process with variance  $\sigma_x^2$ , which can be further extended to non zero mean signal with an arbitrary covariance matrix. We assume additive WGN  $w[n]$ , with variance  $\sigma_\omega^2$ , is independent of signal. The likelihoods corresponding to the two hypotheses can be given as:

$$p(\bar{y}; \mathcal{H}_0) = \frac{1}{(2\pi\sigma_\omega^2)^N} e^{-\frac{\|\bar{y}\|^2}{2\sigma_\omega^2}} \quad (10)$$

$$p(\bar{y}; \mathcal{H}_1) = \frac{1}{(2\pi(\sigma_x^2 + \sigma_\omega^2))^N} e^{-\frac{\|\bar{y}\|^2}{2(\sigma_x^2 + \sigma_\omega^2)}} \quad (11)$$

Where  $\bar{y} = [y[0], y[1], y[2], \dots, y[N-1]]^T$  and N is the number of sample in an observation.

The log LRT gives the test statistics:

$$T[Y] = \sum_{n=0}^{N-1} Y^2[n] = \|\bar{y}\|^2 \quad (12)$$

From (12) the test statistics, is equal to the energy of received signal and hence the name energy detector implies, is a Chi-squared random variable with N degree of freedom. The  $P_{FA}$  and  $P_D$  for an energy detector are calculated as:

$$P_{FA} = P_r\{T(Y) > \gamma'; \mathcal{H}_0\} = Q_{\chi_N^2}\left(\frac{\gamma'}{\sigma_\omega^2}\right) \quad (13)$$

$$P_D = P_r\{T(Y) > \gamma'; \mathcal{H}_1\} = Q_{\chi_N^2}\left(\frac{\gamma'}{\sigma_x^2 + \sigma_\omega^2}\right) \quad (14)$$

Fig.5 shows the theoretical and MATLAB simulated  $P_D$  performance of energy detector for different values of SNR. We note that probability of detection increases monotonically with SNR

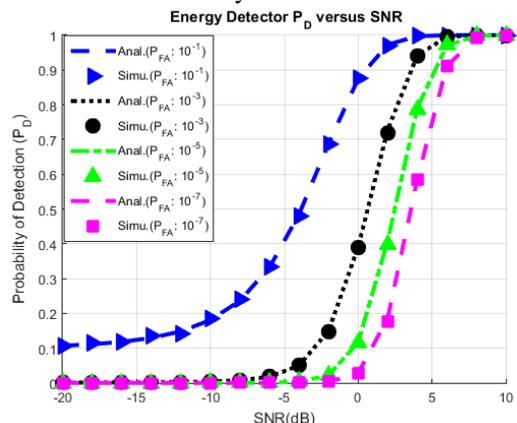


Figure 5: Energy detector  $P_D$  Vs. SNR

From (13) and (14), we get ROC as:

$$P_D = Q_{\chi_N^2}\left(\frac{\sigma_x^2 Q_{\chi_N^2}^{-1}(P_{FA})}{\sigma_x^2 + \sigma_\omega^2}\right) \quad (15)$$

The distribution of energy detector output is central Chi-squared random variable when only noise is present whereas it is noncentral Chi-squared random variable when noise with the unknown signal is present [11]. This characteristic of energy detector ensures the detection of unknown PU with low computational complexity. In [12] a validated model for Energy detector performance in signal uncertainty with noise uncertainty and without noise uncertainty is introduced. This work shows degradation of performance of energy detector in signal uncertainty with noise uncertainty and motivates researchers to study the performance of other techniques under signal uncertainty. In [13] energy detector, for Rayleigh fading channel, based on adaptive sensing scheduling is introduced which utilizes outdated channel state information for spectrum sensing. In [14] energy detection based

spatial spectrum sensing is introduced to overcome the problem of noise uncertainty with lower computational complexity. In [15] effect of in-phase and quarter- phase imbalance(I/Q) is studied on PU performance, and a four-level hypothesis spectrum sensing is introduced to overcome I/Q imbalance.

## V. COMPARISON OF A MATCHED FILTER AND ENERGY BASED SPECTRUM SENSING TECHNIQUES

A matched filter based spectrum sensing technique is employed for only narrowband spectrum sensing whereas energy detector based spectrum sensing employed both for narrowband and wideband spectrum sensing. A matched filter based spectrum sensing has high computational complexity and implementation cost in comparison to the energy detector based spectrum sensing. Being coherent technique in a matched filter based spectrum sensing each SU require PU information storage in its database whereas energy detector has no such information requirements.

## VI. CONCLUSION

As in the development of spectrum sensing techniques, the test statistics,  $ROC$ ,  $P_{FA}$ , and  $P_D$  of the detector are important parameters. Hence first we covered, the mathematical development and MATLAB simulation of these parameters for energy detector and a matched filter based spectrum sensing. A matched filter based spectrum sensing is coherent technique with high computational complexity and implementation cost in comparison to the noncoherent technique, energy detector based spectrum sensing. This survey highlights improvements and introduce new domain to study in detection algorithms.

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