

Implementation of Hybrid CSA, Modified Booth Algorithm and Transient power Minimization techniques in DSP/Multimedia Applications

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Abstract

In Very Large Scale Integration, Low power VLSI design is necessary to meet MOORE'S law and to produce consumer electronics with more back up and less weight. Multiplication occurs frequently in finite impulse response filters, fast Fourier transforms, discrete cosine transforms, convolution, and other important DSP and multimedia kernels. The objective of a good multiplier is to provide a physically compact, good speed and low power consuming chip. To save significant power consumption of a VLSI design, it is a good direction to reduce its dynamic power. In this paper we propose three techniques Hybrid csa, modified booth algorithm and transient power minimization method.. This paper adopts the above three methods in Multiplier, VMFU and multitransform design for H.264(ETD) . In Hybrid csa Method we proposed a new architecture of multiplier-and-accumulator (MAC) for high-speed arithmetic. By combining multiplication with accumulation and devising a hybrid type of carry save adder (CSA), the performance was improved. In Modified booth algorithm technique The modified booth encoder will reduce the number of partial products generated by a factor of 2. In The transient power minimization method SPST adder will avoid the unwanted addition and thus minimize the switching power dissipation. By using these Three techniques We can attain 30% speed improvement and 22% power reduction in Design units of DSP/multimedia Applications. The design units, multiplier, VMFU and ETD plays major role in DSP/Multimedia Applications.

Index terms: Versatile Multimedia Functional Unit (VMFU), Efficient Multi-Transform coding design (ETD), Modified booth encoder (MBE), Spurious Power suppression Technique Equipped Adder (SPST ADDER), Sum of Absolute Difference (SAD), Moore's Law.

Introduction

Power dissipation is recognized as a critical parameter in modern VLSI design field. To satisfy

MOORE'S law and to produce consumer electronics goods with more backup and less weight, low power VLSI design is necessary. Dynamic power dissipation which is the major part of total power dissipation is due to the charging and discharging capacitance in the circuit. The golden formula for calculation of dynamic power dissipation is $P_d = CLV2f$. Power reduction can be achieved by various manners. They are reduction of output Capacitance CL, reduction of power supply voltage V, reduction of switching activity and clock frequency f.

In this section we introduced the above three technologies to encounter the unnecessary power dissipation problems Hybrid CSA is mostly adopted in Multiplier circuits. Modified Booth Encoding is adopted in Multiplier and VMFU. Transient power minimization Method is applicable for Multiplier, VMFU and ETD (H.264)

The method of Hybrid CSA is best understood by applying it to Multipliers [1]. Fast multipliers are essential parts of digital signal processing systems. The speed of multiply operation is of great importance in digital signal processing as well as in the general purpose processors today, especially since the media processing took off. In the past multiplication was generally implemented via a sequence of addition, subtraction, and shift operations. Multiplication can be considered as a series of repeated additions. The number to be added is the multiplicand, the number of times that it is added is the multiplier, and the result is the product. Each step of addition generates a partial product. In most computers, the operand usually contains the same number of bits. When the operands are interpreted as integers, the product is generally twice the length of operands in order to preserve the information content. This repeated addition method that is suggested by the arithmetic definition is slow that it is almost always replaced by an algorithm that makes use of positional representation. It is possible to decompose multipliers into two parts. The first part is dedicated to the generation of partial products, and the second one collects and adds them. The basic multiplication principle is two fold i.e, evaluation of partial products and accumulation of the shifted partial products. It is performed by the successive additions of the columns of the shifted

partial product matrix. The ‘multiplier’ is successfully shifted and gates the appropriate bit of the ‘multiplicand’. The delayed, gated instance of the multiplicand must all be in the same column of the shifted partial product matrix. They are then added to form the product bit for the particular form. Multiplication is therefore a multi operand operation. A general architecture of this MAC is shown in Fig.1. It executes the multiplication operation by multiplying the input multiplier A and the multiplicand B. This is added to the previous multiplication result Z as the accumulation step[13]. The N-bit 2’s complement binary number can be expressed as

$$A = -2^{N-1} a_{N-1} + \sum_{i=0}^{N-2} a_i 2^i, a_i \in 0,1 \dots\dots\dots (1)$$

If (1) is expressed in base-4 type redundant sign digit form in order to apply the radix - 2 Booth’s algorithm.

$$A = \sum_{i=0}^{N/2-2} d_i 4^i \dots\dots\dots (2)$$

$$d_i = -2a_{2i+1} + a_{2i} + a_{2i-1} \dots\dots\dots (3)$$

If (2) is used, multiplication can be expressed as

$$A \times B = \sum_{i=0}^{N/2-2} d_i 2^{2i} B \dots\dots\dots (4)$$

If these equations are used, the afore-mentioned multiplication – accumulation results can be expressed as

$$P = A \times B + Z = \sum_{i=0}^{N/2-2} d_i 2^{2i} B + \sum_{j=0}^{2N-1} z_j 2^j \dots\dots\dots (5)$$

The above equation (5) gives the accumulation process.

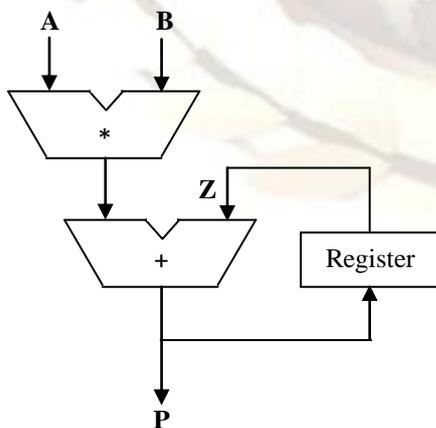


Fig. 1: Accumulation process

The General Multiplication Process

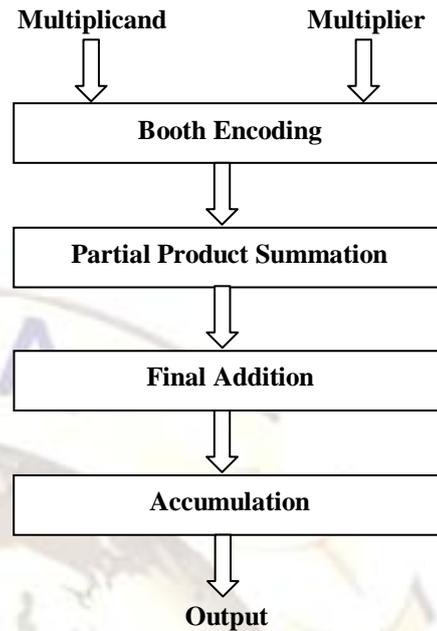


Fig. 2: General Multiplication Process

The Proposed Method of Multiplication

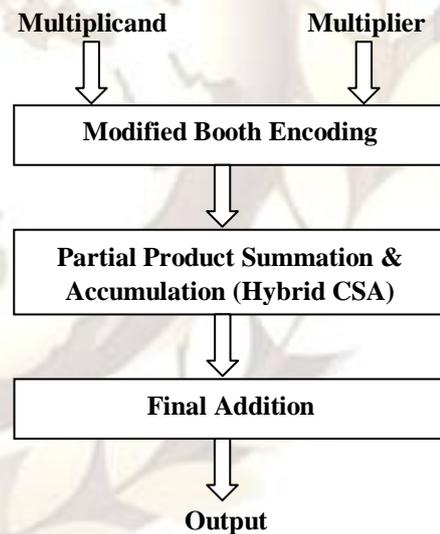


Fig. 3: Multiplication Process by Introducing Hybrid CSA

As shown in the figures (2) and (3) the proposed system requires less power and increases speed of the multiplication process. It also reduces the time consumption[1]-[2].

Modified Booth Encoding Process

A radix-4 modified Booth's algorithm:

Booth's Algorithm is simple but powerful. Speed of MAC is dependent on the number of partial products and speed of accumulate partial product. Booth's Algorithm provide us to reduced partial products. We choose radix-4 algorithm because of below reasons.

➤ Original Booth's algorithm has an inefficient case.

The 17 partial products are generated in 16bit x 16bit signed or unsigned multiplication.

➤ Modified Booth's radix-4 algorithm has fatal encoding time in 16bit x 16bit multiplication.

Radix-4 Algorithm has a 3x term which means that a partial product cannot be generated by shifting. Therefore, 2x + 1x are needed in encoding processing. One of the solution is handling an additional 1x term in wallace tree[3],[6]. However, large wallace tree has some problems too.

A radix-4 modified Booth's algorithm: Booth's radix-4 algorithm is widely used to reduce the area of multiplier and to increase the speed. Grouping 3 bits of multiplier with overlapping has half partial products which improves the system speed. Radix-4 modified Booth's algorithm is shown below:

- X-1 = 0; Insert 0 on the right side of LSB of multiplier.
- Start grouping each 3bits with overlapping from x-1
- If the number of multiplier bits is odd, add a extra 1 bit on left side of MSB
- generate partial product from truth table
- when new partial product is generated, each partial product is added 2 bit left shifting in regular sequence.

The basic idea is that, instead of shifting and adding for every column of the multiplier term and multiplying by 1 or 0, we only take every second column, and multiply by ±1, ±2, or 0, to obtain the same results. The advantage of this method is the halving of the number of partial products[4]. To Booth recode the multiplier term, we consider the bits in blocks of three, such that each block overlaps the previous block by one bit. Grouping starts from the LSB, and the first block only uses two bits of the multiplier. Figure 3 shows the grouping of bits from the multiplier term for use in modified booth encoding[5].

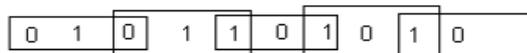


Fig. 4: Grouping of bits from the multiplier term

Each block is decoded to generate the correct partial product. The encoding of the multiplier Y, using the modified booth algorithm, generates the following five signed digits, -2, -1, 0, +1, +2. Each encoded digit in the multiplier

performs a certain operation on the multiplicand, X, as illustrated in Table 1

Block	Re - coded digit	Operation on X
000	0	0 X
001	+1	+1 X
010	+1	+1 X
011	+2	+2 X
100	-2	-2 X
101	-1	-1 X
110	-1	-1 X
111	0	0 X

Transient Power Minimization

Case (1):

$$\begin{array}{r} (128) \quad \boxed{00000000}0 \quad 000000 \\ + (64) \quad \boxed{00000000}01 \quad 000000 \\ (192) \quad \boxed{00000000}1 \quad 000000 \end{array} \quad \longrightarrow \quad \begin{array}{r} (-128) \quad \boxed{11111111}00000000 \\ + (192) \quad \boxed{00000000}10000000 \\ (64) \quad \boxed{00000000}01000000 \end{array}$$

Case (2):

$$\begin{array}{r} (-61) \quad \boxed{11111111}1000011 \\ + (+51) \quad \boxed{00000000}00110011 \\ (-10) \quad \boxed{11111111}1110110 \end{array}$$

Case (3):

$$\begin{array}{r} (-196) \quad \boxed{11111111}00111100 \\ + (204) \quad \boxed{00000000}1001100 \\ (+8) \quad \boxed{00000000}01001000 \end{array}$$

Case (4):

$$\begin{array}{r} (-61) \quad \boxed{11111111}1000011 \\ + (-205) \quad \boxed{11111111}00110011 \\ (-266) \quad \boxed{11111111}1110110 \end{array}$$

Sign $\overleftarrow{\text{carr-ctrl}}$

Case (5):

$$\begin{array}{r} (-196) \quad \boxed{11111111}00111100 \\ + (-52) \quad \boxed{11111111}1001100 \\ (-248) \quad \boxed{11111111}00001000 \end{array}$$

As shown in the above fig. The total power is divided in to MSB POWER and LSB POWER. By using Transient Power minimization technique we can eliminate MSB POWER, Provided Msb data should not Affect the computation[2]. In the Above Figure .The 1st case illustrates a transient state in which the spurious transitions of carry signals occur in the MSP though the final result of the MSP are unchanged. The 2nd and the 3rd cases describe the situations of one negative operand adding another positive operand without and with carry from LSP, respectively. Moreover, the 4th and the 5th cases respectively demonstrate the addition of two negative operands without and with carry-in from LSP. In those cases, the results of the MSP are predictable Therefore the computations in the MSP are useless and can be neglected. The data are separated into the Most Significant Part (MSP) and the Least Significant Part (LSP). To know whether the MSP affects the computation results or not. We need a detection logic unit to detect the effective ranges of the inputs. The Boolean logical equations shown below express the behavioral principles of the detection logic unit in the MSP circuits of the

SPST-based adder/subtractor: The Detection Unit Decides Whether MSB is Allowed or Eliminated. By using this technique we can Suppress Power up to 22%.

Design Unit Multiplier

With the recent rapid advances in multimedia and communication systems, real-time signal processings like audio signal processing, video/image processing, or large capacity data processing are increasingly being demanded. the multiplier and multiplier-and-accumulator (MAC) are the essential elements o the digital signal processings such as filtering, convolution, and inner products. Most digital signal processing methods use nonlinear functions such as discrete cosine transform (DCT) or discrete wavelet transform (DWT)[14].

SPST Equipped Modified Booth Encoding

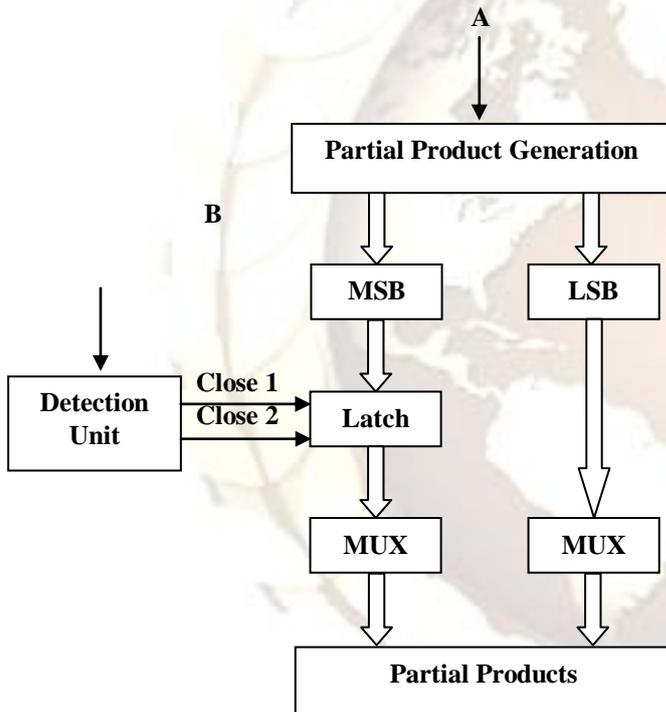


Fig. (5): SPST Equipped Modified Booth Encoding

In this SPST Equipped Modified Booth Encoding the MSB power is suppressed based on the close 1 and close 2 signals. These close 1 and close 2 signals are generated by detection unit. If the MSB part contains all redundant terms, the total MSB power is eliminated by SPST Booth Encoding.

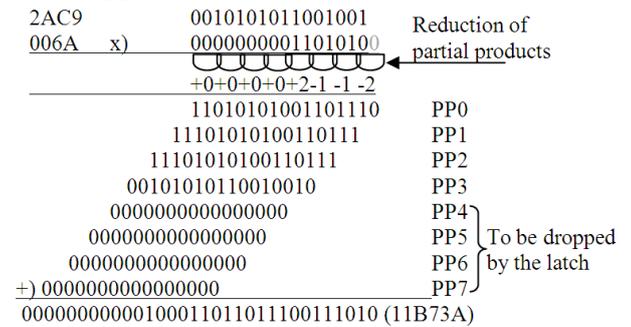
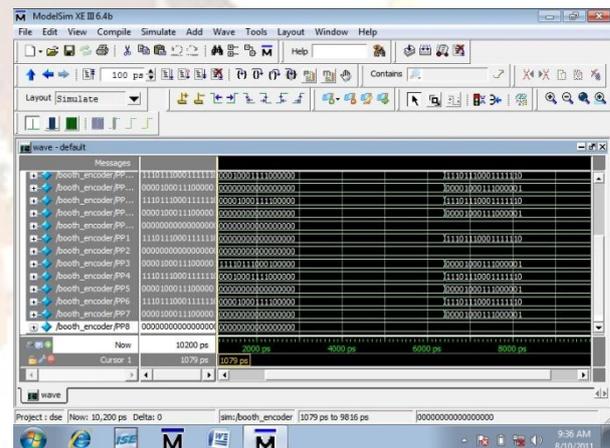


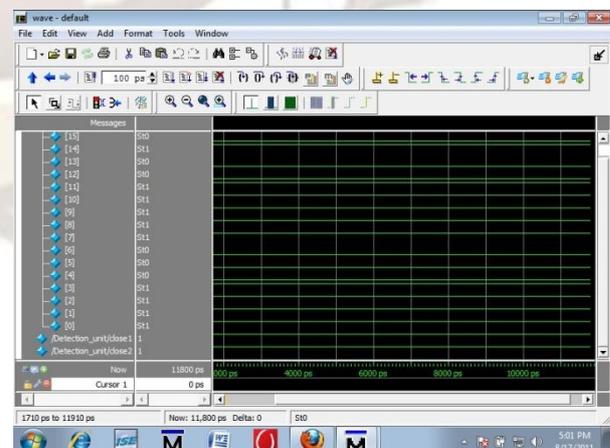
Fig. (6): Illustration of multiplication using modified Booth encoding.

Simulation result of Booth encoding process:

The modified booth encoder is used to generate the partial products and it also used to reduce the number of partial products.



Simulation result of detection unit: Detection unit is used to generate the close 1 and close 2 control signals. These signals decides the whether the MSB part is allowed or not.



The result of final multiplication and accumulation process

time saved from skipping the computations in the MSP circuits shall cancel out the delay caused by the detection-logic unit.

When the detection-logic unit turns on the MSP:

The MSP circuits must wait for the notification of the detection-logic unit to turn on the data latches to let the data in. Hence, the delay caused by the detection-logic unit will contribute to the delay of the whole combinational circuitry, i.e., the 16-bit adder/subtractor in this design example.

When the detection-logic unit remains its decision:

No matter whether the last decision is turning on or turning off the MSP, the delay of the detection logic is negligible because the path of the combinational circuitry (i.e., the 16-bit adder/subtractor in this design example) remains the same. From the analysis earlier, we can know that the total delay is affected only when the detection-logic unit turns on the MSP. However, the detection-logic unit should be a speed-oriented design[2]. When the SPST is applied on combinational circuitries, we should first determine the longest transitions of the interested cross sections of each combinational circuitry, which is a timing

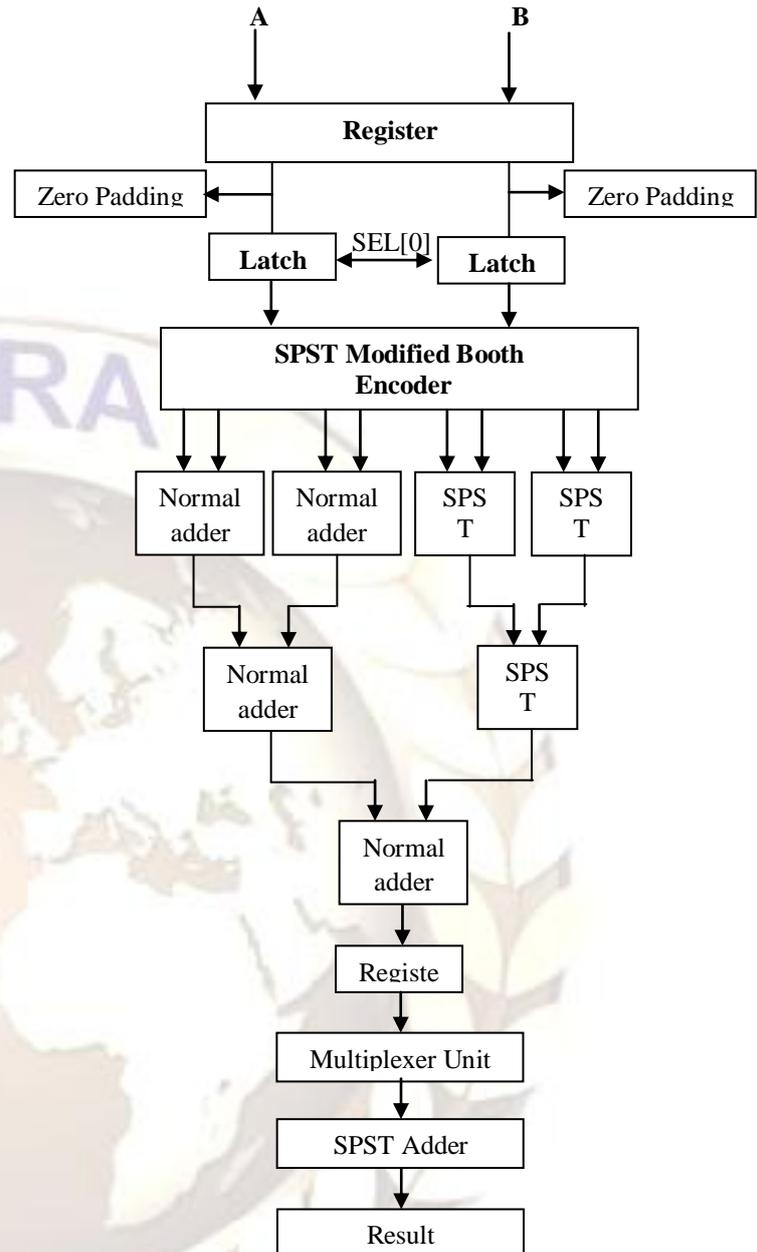
characteristic and is also related to the adopted technology. The longest transitions can be obtained from analyzing the timing differences between the earliest arrival and the latest arrival signals of the cross sections of a combinational circuitry. Then, a delay generator similar to the delay line used in the DLL.

Design unit versatile multimedia functional unit

The proposed VMFU can compute six kinds of arithmetic operations, i.e. addition, subtraction, multiplication, MAC, interpolation, and SAD, which are frequently used in multimedia/DSP computations[2].

This unit takes care of applying the SPST to the Modified Booth Encoder, applying SPST to the Compression Tree and freezing the Switching Activities of the Unused Circuits

Block Diagram of VMFU



Derivation of Multiplier from VMFU

The multiplier circuit can be derived from versatile multimedia functional unit as follows.

By setting selection bits we can achieve Multiplication process. If the selection bits are 001 the operation is Multiplication. The below figure shows the derived version of Multiplier.

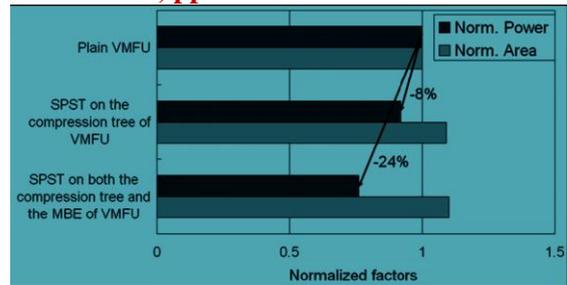
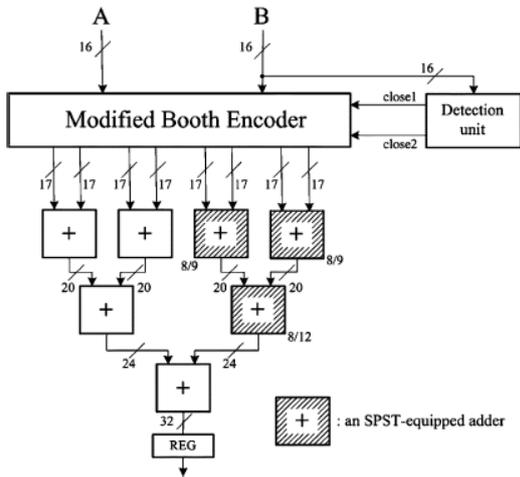


Fig. (8): The power minimization by using SPST equipped VMFU

Based on the selection values the VMFU performs six operations this method consist of three stages [2],[7].

- 1) Partial product generation
- 2) Partial product reduction
- 3) Accumulation process

If the selection bits are 100 the operation is SAD[7].

If the selection bits are 000 the operation is Addition

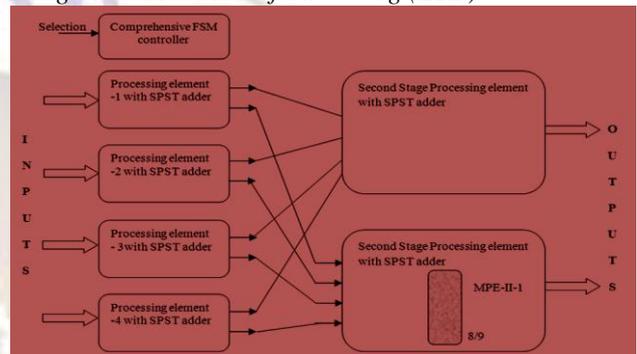
If the selection bits are 010 the operation is Subtraction

If the selection bits are 110 the operation is Interpolation

If the selection bits are 001 the operation is Multiplication

If the selection bits are 111 the operation is MAC

Design Unit Multi Transform coding (ETD)



The efficient multi transform coding (ETD) is generally used for video processing applications in this technique the SPST adders are merged with multiprocessing elements (MPE). Hence we can reduce the power and save the time. Generally these SPST adders equipped in alternate stages because the nice occurred in the first stage is eliminated by the next stage.

Spst equipped multi transform coding:

By combining spst and ETD ,we can get good results.the below diagram shows the above case.Here we discussed the three design units of DSP/Multimedia area.

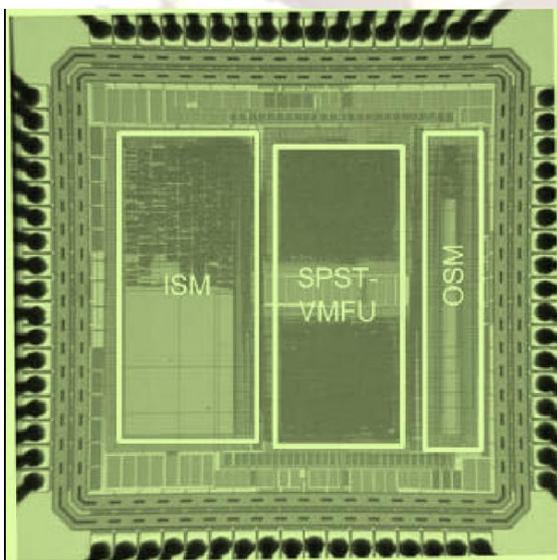


Fig. (7): Chip micrograph of the SPST equipped VMFU

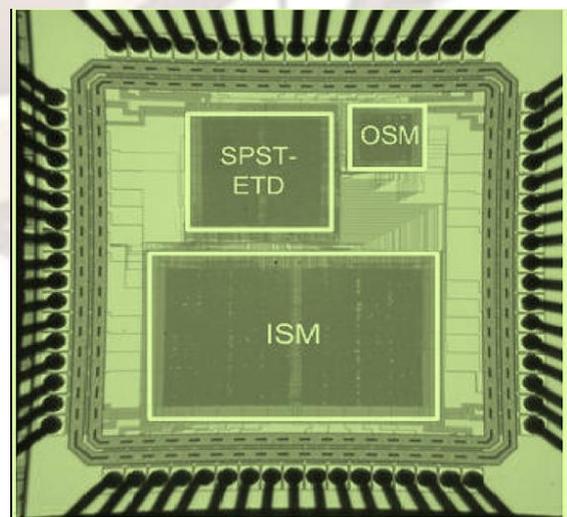


Fig. (9): Chip micrograph of the SPST-ETD

Comparison analysis
Comparison values of multiplier

TABLE I
CHARACTERISTICS OF CSA

Parameter	Existing system	proposed system
Number system	2's complement	1's complement
Sign extension	used	Not used
Accumulation	Result of final addition	Sum and carry of csa
Csa tree	Fa,ha	Fa,ha,2 bit cla
Final adder	2n bits	N bits

- Fa Full adder
- Ha.....Half adder

TABLE II
CALCULATION OF HARDWARE RESOURCE

Components	Existing		Proposed	
	General	16 bits	General	16 bits
Fa	$(n^2/2+n)$	964.8	$(n^2/2+n/2)$	911.2
Ha	0	0	$3n/2$	76.8
2 bit cla	0	0	$n/2$	56
Accumulator	$(2n+1)$	214	-	-
Final adder	2n bits	197	N bits	97
Total		1375.8		1141

- n---Number of bits
- Fa—Full adder
- Ha—Half adder

TABLE III
GATE SIZE OF LOGIC CIRCUIT ELEMENT

S.no	Element	Gate size
1	Inveter	0.8
2	2/3/4- nand	1/1.5/2.5
3	2/3/4- nor	1/2/2.2
4	2/3/4-xor	2/4/6
5	2/3/4-and	1.2/1.5/2
6	2/3/4-or	1.2/1.5/2
7	Half adder	3.2
8	Full adder	6.7
9	D flip-flop	6.2
10	4×1 mux	6
11	8×1 mux	14.2
12	2 bits cla	7
13	4 bits cla	20.5

TABLE IV
PIPELINE STAGE

Stage	Existing	Proposed
Stage1	$139.95n+1$	$44.15n+1$
Stage2	$57.2n+28.5$	$28.6n$

TABLE V
PIPELINE AND PERFORMANCE ANALYSIS

Item	Existing	The proposed
Output rate	2 clocks	1 clock
Pipeline delay	$139.9n+87.1$	$44.15n+81.1$

TABLE VI
NORMALIZED CAPACITANCE AND GATE DELAY

Gate	Comment	Capacitance	Gate delay
Inverter	-	3	T+c
8×1 mux	4-level logic	4	35.2+t+c
D –f/f	Slave delay	4	16.1+t+c
1 bit fa	Input-to sum	12	39.6+t+c
1 bit fa	Input –to-carry	12	38.7+t+c
2 bit cla	Input-to sum	12	64.9+t+c
2 bit cla	Input-to-carry	16	53.9+t+c
4 bit cla	Input-to sum	12	96.8+t+c
4 bit cla	Input –to-carry	24	88+t+c

TABLE VII
COMPARISION BETWEEN EXISTING AND THE PROPOSED

Parameter	Existing	Proposed
Step1	Booth encoding	Booth encoding
Step2	Csa	Hybrid csa
Step3	Final addition	Final addition
Step4	Accumulation	---
Critical path	915.2	536.8
Spst adder	Not implemented	Implemented

TABLE VIII
POWER COMPARISON BY USING TRANSIENT POWER MINIMIZATION METHOD

Frequency	Power(mw)		Reduction (%)
	Spst on	Spst off	
22	5.49	7.57	27.48
50	12.05	16.59	27.37
100	24.18	33.25	27.28

Conclusion

In this paper, we discussed the implementation of modified booth algorithm, hybrid CSA and transient minimization power techniques for the design units multiplier, VMFU and ETD. By using modified booth encoding technique we can increase the speed of the system and by using Power transient minimization method we can reduce the power up to 24%. By combining CSA and accumulation process we can form a hybrid CSA, which is the most suitable application of multiplier.

Future scope

By using Transient power minimization method, we can reduce the power consumption. But this technique increases the chip area, due to incorporation of detection unit. If we suppress the LSB power also we can further decrease the power consumption. By applying Alpha power theorem and LSB power minimization technique we can compensate the Augumentation of Area.

References

[1] New vlsi architecture of parallel multiplier-accumulator based on radix-2 modified booth algorithm
Ho Seo and Dong-Wook Kim,IEEE
Volume 18,No2 Feb 2010

[2] A Spurious power suppression Technique for multimedia/Dsp applications,IEEE Transations,Vol 56,No.1, Kuan-Hung Chen,Yuan-Sun Chu.

[3] C. S. Wallace, "A suggestion for a fast multiplier," *IEEE Trans. Electron Comput.*, vol. EC-13, no. 1, pp. 14–17, Feb. 1964.

[4] A. R. Cooper, "Parallel architecture modified Booth multiplier," *Proc. Inst. Electr. Eng. G*, vol. 135, pp. 125–128, 1988.

[5] N. R. Shanbag and P. Juneja, "Parallel implementation of a 4×4-bit multiplier using modified Booth's algorithm," *IEEE J. Solid-State Circuits*, vol. 23, no. 4, pp. 1010–1013, Aug. 1988.

[6] J. Fadavi-Ardekani, "M₀N Booth encoded multiplier generator using optimizedWallace trees," *IEEE Trans. Very Large Scale Integr. (VLSI)Syst.*, vol. 1, no. 2, pp. 120–125, Jun. 1993.

[7] N. Ohkubo, M. Suzuki, T. Shinbo, T. Yamanaka, A. Shimizu, K.Sasaki, and Y. Nakagome, "A 4.4 ns CMOS 54×54 multiplier using pass-transistor multiplexer," *IEEE J. Solid-State Circuits*, vol. 30, no.3, pp. 251–257, Mar. 1995.

- [8] A. Tawfik, F. Elguibaly, and P. Agathoklis, "New realization and implementation of fixed-point IIR digital filters," *J. Circuits, Syst., Comput.*, vol. 7, no. 3, pp. 191–209, 1997.
- [9] A. Tawfik, F. Elguibaly, M. N. Fahmi, E. Abdel-Raheem, and P. Agathoklis, "High-speed area-efficient inner-product processor," *Can. J. Electr. Comput. Eng.*, vol. 19, pp. 187–191, 1994.
- [10] F. Elguibaly and A. Rayhan, "Overflow handling in inner-product processors," in *Proc. IEEE Pacific Rim Conf. Commun., Comput., Signal Process.*, Aug. 1997, pp. 117–120.
- [11] F. Elguibaly, "A fast parallel multiplier–accumulator using the modified Booth algorithm," *IEEE Trans. Circuits Syst.*, vol. 27, no. 9, pp.902–908, Sep. 2000.
- [12] A. Fayed and M. Bayoumi, "A merged multiplier-accumulator for high speed signal processing applications," *Proc. ICASSP*, vol. 3, pp.3212–3215, 2002.
- [13] P. Zicari, S. Perri, P. Corsonello, and G. Cocorullo, "An optimized adder accumulator for high speed MACs," *Proc. ASICON 2005*, vol.2, pp. 757–760, 2005.
- [14] T. Sakurai and A. R. Newton, "Alpha-power law MOSFET model and its applications to CMOS inverter delay and other formulas," *IEEE J.Solid-State Circuits*, vol. 25, no. 2, pp. 584–594, Feb. 1990.
- [15] A. D. Booth, "A signed binary multiplication technique," *Quart. J.Math.*, vol. IV, pp. 236–240, 1952.



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